

Skills, innovation, and growth: An agent-based policy analysis ^{*}

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Abstract

We develop an agent-based macroeconomic model featuring a distinct geographical dimension and heterogeneous workers with respect to skill types. The model, which will become part of a larger simulation platform for European policymaking (EURACE), allows us to conduct ex-ante evaluations of a wide range of public policy measures and their interaction. In particular, we study the growth and labor market effects of various policy types that promote workers' general skill levels. It is examined in how far effects differ if spending is uniformly spread over all regions in the economy or focused in one particular region. We find that the geographic distribution of policy measures significantly affects the effects of the policy even if total spending is kept constant. Focussing training efforts in one region is the worst policy outcome while spreading funds equally across regions generates a larger output in the long-run but not in the short-run.

1 Introduction

Normative research in economics has traditionally been, and to a large degree still is based on the development and analysis of highly stylized, analytically tractable models. In particular for macroeconomic issues the models used for policy analysis are typically dynamic general equilibrium models that

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have been calibrated using empirical data. However, numerous restrictive assumptions underly most mainstream analytical models (e.g. homogeneity of individuals, perfect rationality, rational expectations, perfect ex-ante coordination in an equilibrium) and so far there exists almost no general theoretical basis that allows to judge how far findings, obtained under these simplifying assumptions, carry over to scenarios where agents are heterogeneous or out of equilibrium (see e.g. Kirman (1992)). On the other hand, recent developments in computer technology and software engineering have made large scale simulations an increasingly powerful and attractive new approach for understanding the characteristics of economic systems and for deriving economic policy recommendations. In particular, by explicitly modelling the decentralized interaction of heterogeneous economic agents in systems like markets or organizations, *agent-based computational economics* (ACE) attempts to transcend the limitations of traditional models.

The ACE modeling approach is not only well suited for explicit consideration of heterogeneity among economic agents, but also allows for a wide range of assumptions concerning the rules that determine the behavior of individual economic agents. Existing ACE models typically consider adaptive individuals who learn how to behave and react based on their own experience and on the available information¹. Models of this kind have been developed in many areas of economics. Among others, they have been used to study the emergence of trading behavior on goods-markets and on financial markets, bidding behavior in auctions, numerous issues concerning innovation and industry evolution or the emergence of cooperative behavior in economic systems. Surveys over agent-based research in these areas can be found in Tesfatsion and Judd (2006).

A major advantage of the agent-based simulation approach is that the modeler can easily study the effects of changes in the economic framework on various aspects of the resulting economic dynamics and long run outcome. Accordingly, agent-based models have a large potential as a tool to evaluate the impact of public policy measures or of changes in market design. Whereas early ACE-work has been mainly of descriptive character, in recent years there have been a number of projects where agent-based models have been employed to (normatively) address actual market design and public policy questions (see e.g. Dawid and Fagiolo (2007)). The considered policy issues relate to electricity markets (e.g. Bunn and Oliveira (2001), Nicolaisen et al. (2001)), labor market design (e.g. Neugart (2007)), auction design (e.g. Phelps et al. (2002)), patent policy (e.g. Malerba et al. (2001))

¹Work by Cyert and March (1963), Simon (1978, 1983) or Nelson and Winter (1982) has been influential for the development of this line of research.

or agricultural policy (e.g. Happe et al. (2007)). This list of issues demonstrates that so far the focus of agent-based normative analysis has been on questions of market-design and have typically involved partial models of particular markets. Agent-based work in the area of macroeconomic modelling is however sparse. Closed macroeconomic models using an ACE approach have been provided for example by Chiaromonte and Dosi (1993), Silverberg and Verspagen (1993), Delli Gatti et al. (2005), and Dosi et al. (2006). But the focus of this work is on demonstrating that the models are able to simultaneously reproduce a large number of empirically observable stylized facts rather than on the evaluation of economic policy measures.

The purpose of this paper is to demonstrate that agent-based closed macroeconomic models are not only well suited to reproduce empirically observed regularities but can be usefully applied to evaluate economic policy measures in a way that is infeasible for representative agent models. In particular, we focus on an area that has recently received strong attention by policy makers in industrialized countries, namely the question what kind of economic policy measures are best suited to facilitate innovation and diffusion of new technologies and productivity increase. Dealing with this question requires to shed more light on the interplay of processes leading to the generation of new technologies and the ability of firms to adopt such new technologies. In order to efficiently use new technologies the workforce of the industrial firms has to be able to build up the required level of specific skills and the ability to do so depends on the general skills levels of the employees. There is strong empirical evidence that the skill distribution in the workforce has substantial influence on the speed of technological change, the employment and wage dynamics and growth in an economy (e.g. Bassanini and Scarpetta (2002), Bassanini (2004)). For example empirical studies initiated by the OECD economics division (see e.g. OECD (2000)) indicate that the lack of the new forces of economic growth and relatively low-skill levels in the labor force have negative effects on employment in Europe. In particular, the U.S. took the lead since the 1990's in creating new knowledge, human capital and innovations accompanied by entrepreneurship and new start-up firms which gave rise to higher employment. Therefore, policies aiming at a change in the local skill distribution play an important role in fostering technological change and growth. Any model designed to evaluate such policies, and more generally any technology and growth policy measures, miss a crucial aspect if they do not incorporate the dynamics of skill and knowledge distribution in the workforce.

In that respect spatial aspects also play a crucial role. First, in many industrialized countries there are strong regional differences in the skill and knowledge distribution where high-skill employees are strongly concentrated

in a few areas. Second, geographic proximity between firms has a crucial impact on the intensity of technological spillovers between them. Both theoretical and empirical studies of innovative activities have demonstrated the importance of technological spillovers for industry development (see e.g. the surveys by Audretsch and Feldman (2004) and Döring and Schnellenbach (2006)). Whereas the main channels through which technological information flows between firms depends heavily on the type of industry considered (see e.g. Geroski (1995)), a considerable role in establishing technological spillovers is typically assigned to direct communication and the flow of skilled and well informed employees. Therefore, the interaction of firms and employees on the (local) labor market is of great importance for the size of technological spillovers and, hence, for innovative activities. Taking into account regional differences and the existence of (*local*) knowledge flows between firms the question arises to what extent economic policy measures should be regionally differentiated. In particular, it has to be explored how the effects of certain skill enhancing policy measures differ when applied in regions with different characteristics. Furthermore, the right allocation of policy measures among all regions in the economy is a difficult problem. Should the activity be centered on the strongest or on the weakest region or should all measures be uniformly distributed across regions?

In previous years the main approach for the analysis of spatial aspects of economic activity has been the use of 'New Economic Geography' (NEG) models introduced by Krugman (1991). These models rely on a number of simplifying assumptions like the restriction to two regions or equidistant multi-regions (see Bosker et al. (2007)), the absence of strategic behavior of firms or the lack of considerations of institutional aspects. These restrictions, which are mainly due to the desire to keep the models tractable, have been acknowledged by NEG researchers. For example in their survey of recent NEG work Ottaviano and Thisse (2004) point out that '*By their very nature, such models are unable to, explain the rich and complex hierarchy that characterizes the space-economy. . . . Therefore, one major step on the research agenda is the study of a multi-regional system whose aim is to understand why some regions are more successful than others.*' [p. 2603]. Also some limitations of NEG concerning the study of spatial dynamics on the labor market is acknowledged in Ottaviano and Thisse (2004): '*Another fundamental question is related to the fact that local labor markets are modeled in a very simple way in NEG: operating profits are used to pay skilled workers. In particular, these models do not help understand why unemployment persists in areas included in or adjacent to prosperous regions.*' [p. 2604]. These restrictions of NEG models imply that they are not well suited to address the (spatial) policy questions discussed above. Actually, the work using an NEG approach for

normative analysis of economic policy is limited. An indicator in that respect is that the recently published Handbook of Regional and Urban Economics (Henderson and Thisse (2004)), where a lot of attention is dedicated to NEG, does not include any chapters discussing economic policy.

Based on the obvious restrictions imposed by analytical tractability on the spatial analysis of the interplay of technological change and properties of the labor force, the need for an alternative approach for the evaluation of different combinations of economic policy measures seems particularly strong. Agent-based models are well suited to address this need². In this paper we sketch an agent-based model that is as simple as possible but still apt to address some of the important policy questions raised above. It is a closed model consisting of a consumption goods and an investment (or capital) goods sector. Households and firms are distributed across regions. Some markets (consumption goods) are assumed to be local, some are global (investment goods) and workers might commute for work to employers in neighboring regions at certain costs. Investment goods are supplied at an exogenously given price. The inputs for consumption good production are investment goods and labor. Process innovation improves the quality of investment goods leading to higher productivity of capital in the consumption good production. The labor market hosts workers of different types. They are differentiated along their general as well as their specific skill level. A crucial assumption is that sufficient specific skills of workers are needed to exploit the full potential of the advanced technological level of investment goods like production machines. Put formally, there is complementarity between the average quality of the investment goods of a firm and the average level of specific skills of its employees with respect to the productivity in consumption good production. Empirical evidence for such complementarity can for example be found in Griffith et al. (2004). Workers of higher general skills adapt faster in terms of their specific skills needed to produce consumption goods by the use of investment goods of a particular quality. General skills affecting the adaptation of specific skills will allow us to study the effects of government policies improving the general skill level of the workforce on employment and growth.

A general problem of agent-based models, that attempt to avoid the (overly) strong assumptions about information and rationality of individuals underlying equilibrium analysis, is the appropriate design of decision rules that govern the behavior of individual agents. Deviation from the intertemporal (constrained) maximization paradigm opens many degrees of freedom

²See Dawid and Wersching (2006) or Wersching (2007) for agent-based analyses of spatial aspects of industry dynamics.

with respect to the type of behavioral rules used and the way behavior is adapted over time. However, as far as firm behavior is concerned for many operational decisions, like pricing, production and inventory choice or market selection decisions, standard decision rules and heuristics have been developed that are well documented in the relevant business and operations management literature. Our ‘philosophy’ in terms of modelling firm behavior is to implement relatively simple decision rules that match standard procedures of real world firms as described in the corresponding management literature. In a similar spirit the decisions of consumers, like the allocation of the available budget between consumption and savings, is modelled according to simple empirically founded rules from the literature.

Apart from the fact that behavioral rules of individual agents in the model have to be in accordance with stylized representations of standard decision rules employed by their real-world representatives, it is also important to critically examine the plausibility of the qualitative patterns of simulation results. A widely used approach for this kind of model evaluation in recent work in agent-based economics is to compare simulation outcomes with ‘stylized facts’ that have been established using real world data. This kind of comparison is supposed to restrict the range of model parameters and to improve the confidence that the model captures crucial aspects of interactions in the sectors considered in the model, see Windrum et al. (2007) for a discussion of approaches to validate agent-based simulation models. Due to space constraints we only sketch such empirical validation of our model here and rather focus on the presentation of the economic logic exhibited by our policy experiments.

The strong empirical footing of the developed agent-based model is not only of great importance for purely scientific reasons but is also crucial to establish trust of actual policy makers in the results of the policy analysis and the policy recommendations generated by the model. The model and preliminary analysis presented in this paper is part of the EU-funded project (EURACE) ‘An Agent-based Software Platform for European Economic Policy Design with Heterogeneous Interacting Agents: New Insights from a Bottom-Up Approach to Economic Modeling and Simulation’³. The main purpose of the project is to develop a unified agent-based macroeconomic simulation platform that can be used to inform policy makers about expected effects of (combinations of) various economic policy measures. Our focus here is on industrial and labor-market issues, but the goal of the entire project is to cover all main areas of economic policy.

³See <http://www.eurace.org> or <http://www.wiwi.uni-bielefeld.de/~dawid/eurace/> for more information about the EURACE project.

We proceed as follows. The main features of the simulation model are described in section 2. In section 3 we briefly present key features of simulation results generated by the model and then discuss the potential of the framework to evaluate different types of policy measures that aim at faster economic growth. The potential of the model for policy analysis is then illustrated by comparing the effects of different degrees of spatial concentration of policy measures. We conclude in section 4 with a brief discussion and pointers to future work.

2 The model

2.1 General features

Our model consists of a capital good, a consumption good, and a labor market.⁴ Capital goods are provided with infinite supply at exogenously given prices. The quality of the capital good improves over time where technological change is driven by a stochastic (innovation) process. Firms in the consumption goods sector use capital goods combined with labor input to produce consumption goods. The labor market is populated with workers that have a finite number of general skill levels and acquire specific skills on-the-job which they need to fully exploit the technological advantages of the capital employed in the production process. Consumption goods are sold at malls. Malls are not treated as profit-oriented enterprises but simply as local market platforms where firms store and offer their products and consumers come to buy goods at posted prices.

Thus, two types of active agents and two types of passive agents (in the sense that this type of agent does not take any decisions) are present in the model. Each type of active agent has several ‘roles’ corresponding to its activities in the different markets. Table 1 summarizes these roles.

The economy consists of $R = 2$ regions and each agent is located in one of these regions. Some actions occur locally, such as the agents’ consumption, others occur globally including the sale of the investment good or labor supply.

Generally, the minimal unit of time is a day, however almost all the interactions and decisions are repeated on a monthly basis.⁵ Therefore, whenever

⁴In the fully fledged EURACE model, a financial and a credit market will be added, and an exogenous energy market will constitute a proxy for the link to the ‘rest-of-the-world’ by affecting the production costs in the capital goods market.

⁵In the model each week consists of 5 days and each month of 4 weeks. Accordingly, each year has 240 days.

Active Agents	Households	- Consumption Goods Market: Role of Buyer - Labor Market: Role of Worker
	Consumption Goods Producer	- Investment Goods Market: Role of Buyer - Consumption Goods Market: Role of Seller - Labor Market: Role of Employer
Passive Agents	Malls	- Consumption Goods Market: Information Transfer between Producers and Households
	Capital Goods Producer	- Investment Goods Market: Role of Seller

Table 1: Agents and their role in the model.

we refer to one time-period by default we mean one month. Some decisions in the consumption goods market are taken on a weekly basis and we will explicitly point out this fact in the text.

2.2 Investment goods market

There exists a single type of technology for investment goods. The investment good is offered with infinite supply. The quality of the investment good q_t^{inv} increases over time due to a stochastic process. Every period the quality is increased with probability $\gamma^{inv} \in (0, 1)$ and in case of an increase the quality of the offered good changes by a fixed percentage Δq^{inv} .

The price of the investment good $p^{inv} > 0$ is assumed to be linked to the level of quality, so that a rise of quality leads to a proportional increase of p^{inv} . Although capital goods producers are not modelled as active agents the amounts paid for investment goods are channelled back into the economy. Revenues accruing with the investment good producer are distributed in equal shares among all households in order to close the model. Put differently, it is assumed that all households own equal shares in the fictitious capital goods producer.

2.3 Consumption good producer

2.3.1 Quantity choice

Every consumption goods producer keeps a stock of its products at every regional mall. For simplicity it is assumed that all producers offer their products in both regions. A producer checks once every period whether any of the stocks it keeps at different malls have to be refilled. To that end the

firm receives messages from all the malls it serves reporting the current stock level. Taking this information into account, the firm i has to decide whether and on what scale it restocks the supply. According to our approach of using standard managerial methods wherever it is applicable, we employ a standard inventory rule for managing the stock holding. For reasons of simplicity we ignore setup costs that arise for each delivery to a mall. We denote by $C_{i,r}^{inv}$ costs of holding one unit of the good in the inventory for one period and by $\tilde{\Phi}_{i,r,t}(D) : [0, \infty) \mapsto [0, 1]$ the estimated distribution function of the demand for the good of firm i at the mall in region r , where the estimation is based on demands reported by the mall in the previous T periods. Furthermore, $SL_{i,r,t}$ is the level of the stock of firm i at the mall in region r at the day in period t when the stock is checked. Then, standard results from inventory theory suggest that the firm should choose its desired replenishment quantity for region r according to the following simple rule (see Hillier and Lieberman (1986)):

$$\tilde{D}_{i,r,t} = \begin{cases} 0 & SL_{i,r,t} \geq Y_{i,r,t} \\ Y_{i,r,t} - SL_{i,r,t} & SL_{i,r,t} < Y_{i,r,t}, \end{cases}$$

where $Y_{i,r,t}$ is the smallest value $Y \geq 0$ that satisfies

$$\tilde{\Phi}_{i,r,t}(Y) \geq \frac{p_{i,r,t} - (1 - \rho)\bar{c}_{i,t-1}}{p_{i,r,t} + C_{i,r}^{inv}}.$$

Here $\bar{c}_{i,t-1}$ denotes unit costs of production for firm i in the previous period, $p_{i,r,t}$ the prices of the consumption good, and ρ the discount factor. The sum of the orders received by all malls becomes

$$\tilde{D}_{i,t} = \sum_{r=1}^R \tilde{D}_{i,r,t}.$$

To avoid excessive oscillations of the quantities $\tilde{Q}_{i,t}$ that the firm desires to produce in period t , the time-series of total quantities required by the different malls ($\tilde{D}_{i,t}$) is smoothed. On this account, the consumption goods producer shows some inertia in adapting the actual production quantity to the quantity requested by the malls. In particular, we have

$$\tilde{Q}_{i,t} = \xi \cdot \tilde{D}_{i,t} + (1 - \xi) \cdot \frac{1}{T} \cdot \sum_{k=t-T}^{t-1} Q_{i,k}.$$

As discussed in more detail below, the realized production volume $Q_{i,t}$ can deviate from the planned output $\tilde{Q}_{i,t}$ due to rationing on the factor markets.

The quantities actually delivered to the malls, $D_{i,r,t}$, are adjusted proportional to the intended quantities $\tilde{D}_{i,r,t}$, so that

$$D_{i,r,t} = \frac{\tilde{D}_{i,r,t}}{\sum_{r'=1}^R \tilde{D}_{i,r',t}} \cdot Q_{i,t}.$$

Production times of consumption goods are not explicitly taken into account and the produced quantities are delivered on the same day when production takes place. The local stock levels at the malls are updated accordingly.

2.3.2 Factor demand

Consumption good producers, denoted by i , need physical capital and labor to produce the consumption goods. The accumulation of physical capital by a consumption good producer follows

$$K_{i,t+1} = (1 - \delta)K_{i,t} + I_{i,t}$$

where $K_i(0) = 0$ and $I_{i,t} > 0$ is the gross investment.

Every worker w has a level of general skills $b_w^{gen} \in \{1, \dots, b_{max}^{gen}\}$ and a level of specific skills $b_{w,t}$. The specific skills of worker w indicate how efficiently the corresponding technology is exploited by the individual worker. Building up those specific skills depends on collecting experience by using the technology in the production process. There is vast empirical evidence for such adjustment processes (see e.g. Argote and Epple (1990)). The shape of the evolution of productivity follows a concave curve, the so-called learning curve, when the organizational productivity is recorded after implementing a new production method or introducing a new good. Concavity in this context means that the productivity rises with proceeding use of the production method or production of the new good, but this increase emerges at a decreasing rate. We transfer this pattern of organizational learning on the individual level and assume that the development of individual productivity follows a learning curve. The specific skills are updated once in each production cycle of one month. Further, we assume that updating takes place at the end of the cycle.

A crucial assumption is the positive relationship between the general skills b_w^{gen} of a worker and his ability to utilize his experiences. Building up worker's technology specific skills depends on a worker's level of general skills, i.e. his education and the other abilities which are not directly linked to the particular technology. Taking the relevance of the general skill level into account the specific skills of a worker w for technology j is assumed to evolve according to

$$b_{w,t+1} = b_{w,t} + \chi(b_w^{gen}) \cdot (A_{i,t} - b_{w,t}),$$

where we denote with $A_{i,t}$ the average quality of the capital stock. The function χ is increasing in the general skill level of the worker. Note that this formulation captures the fact that in the absence of technology improvements marginal learning curve effects per time unit decrease as experience is accumulated and the specific skills of the worker approaches the current technological frontier.

The production technology in the consumption goods sector is represented by a Cobb-Douglas type production function with complementarities between the quality of the investment good and the specific skills of employees for using that type of technology. Factor productivity is determined by the minimum of the average quality of physical capital and the average level of relevant specific skills of the workers. Capital and labor input is substitutable with a constant elasticity and we assume constant returns to scale. Accordingly, output for a consumption goods producer is given by

$$Q_{i,t} = \min[B_{i,t}, A_{i,t}] \times L_{i,t}^\alpha K_{i,t}^\beta,$$

where $B_{i,t}$ denotes the average specific skill level in firms and $\alpha + \beta = 1$.

Firms aim to realize a capital to labor ratio according to the standard rule for CES production functions. That is a ratio of quantity to price of the two factors proportional to the corresponding intensity parameter. Accordingly,

$$\frac{\tilde{K}_{i,t}}{p^{inv}} / \frac{\tilde{L}_{i,t}}{w_t^e} = \frac{\beta}{\alpha}.$$

Taking into account the above production function this yields under the assumption of positive investments

$$\begin{aligned} \tilde{K}_{i,t} &= \frac{(\beta w_t^e)^\alpha \tilde{Q}_{i,t}}{(\alpha p^{inv})^\alpha \min[A_{i,t}, B_{i,t}]} \\ \tilde{L}_{i,t} &= \frac{(\alpha p^{inv})^\beta \tilde{Q}_{i,t}}{(\beta w_t^e)^\beta \min[A_{i,t}, B_{i,t}]} \end{aligned}$$

and if $\tilde{K}_{i,t} \geq (1 - \delta)K_{i,t-1}$ the desired capital and labor stocks read $\tilde{K}_{i,t} = \tilde{K}_{i,t}$ and $\tilde{L}_{i,t} = \tilde{L}_{i,t}$. Otherwise, we have

$$\begin{aligned} \tilde{K}_{i,t} &= (1 - \delta)K_{i,t-1} \\ \tilde{L}_{i,t} &= \left(\frac{(\tilde{Q}_{i,t})}{((1 - \delta)K_{i,t-1})^\beta \min[A_{i,t}, B_{i,t}]} \right)^{1/\alpha}. \end{aligned}$$

For simplicity credit constraints are not incorporated in this version of the model.⁶ All desired investments can be financed.

The monthly realized profit of a consumption goods producer is the difference of sales revenues achieved in the malls during the previous period and costs as well as investments (i.e. labor costs and capital good investments) borne for production in the current period. In cases of positive profits, the firm pays dividends to its stockholders and the remaining profits, as well as losses, are entered on an account $Acc_{i,t}$. Similar to the capital goods producer, we assume that all households hold equal shares in all consumption goods producers, consequently the dividends are equally distributed to the households. In order to avoid exceeding accumulations of savings as well as excessive indebtedness, we employ a simple dividend policy that provides different dividend rates depending on the current balance of saving account $Acc_{i,t}$. The rule states that a firm pays no dividends, if the balance is negative and the debt is on a scale above the last monthly revenue. If the balance is positive and savings are above the monthly revenue, the firm disburses all profits. In the remaining case, if the balance is between these critical levels, a fixed proportion $div \in [0, 1]$ of profits is paid out.

Since there are no constraints on the credit market and there is infinite supply of the investment good, the consumption goods producers are never rationed on the investment goods market. Wages for the full month are paid to all workers at the day when the firm updates its labor force. Investment goods are paid at the day when they are delivered.

2.3.3 Pricing

Consumption good producers employ a standard approach from the management literature, the so-called ‘break-even analysis’ (see Nagle (1987)), to set their prices. The break-even formula determines at what point the change in sales becomes large enough to make a price reduction profitable and at what point the decrease in sales becomes small enough to justify a rise in the price. Basically, this managerial pricing rule corresponds to standard elasticity based pricing.

Assuming that all firms have constant expectations $\varepsilon_i^e < -1$ of the elasticity of their demand, they set the price according to the standard rule

$$p_{i,t} = \frac{\bar{c}_{i,t-1}}{1 + 1/\varepsilon_i^e},$$

where $\bar{c}_{i,t-1}$ denotes unit costs in production of firm i in the previous period.

⁶In contrast, in the fully fledged EURACE platform, there is an explicit credit market model which can be appropriately linked to the real sectors considered here.

Once the firm has determined the updated prices $p_{i,r,t}$ for all regions r where it offers its goods, the new prices are sent to the regional malls and posted there for the following period.

2.4 Households' consumption

Once a month households receive their income. Depending on the available cash, that is the current income from factor markets (i.e. labor income and dividends distributed by capital and consumption goods producers) plus assets carried over from the previous period, the household sets the budget which it will spend for consumption and consequently determines the remaining part which is saved. On a weekly basis, sampling prices at the (regional) mall the consumer decides which goods to buy.

2.4.1 The savings decision

Our decision rule for determining the savings is based on the work of Deaton (1991). Deaton examines the saving behavior of impatient consumers when they are not permitted to borrow. In a scenario with independent and identically distributed income draws, he obtains a consumption function depending on cash on hand, which has the following characteristics: There exists a critical value of cash on hand. When the available liquidity is below this critical value the whole cash on hand will be spent. In the opposite case the agent will save a part of his cash on hand.⁷ The assets act like a buffer stock which protect consumption against bad income draws.

We assume a stepwise linear approximation of the consumption rule derived by Deaton (1991, 1992). At the beginning of period t , a consumer k decides about the budget $B_{k,t}^{cons}$ that he will spend. In period t the agent receives an income $Inc_{k,t}$, and holds assets $Ass_{k,t}$. Thus, cash on hand is denoted by $Liq_{k,t}^{Avail} = Ass_{k,t} + Inc_{k,t}$. The assets evolve according to

$$Ass_{k,t} = Liq_{k,t-1}^{Avail} - B_{k,t-1}^{cons}.$$

Note, that while we do not establish interest rates here, in the fully fledged EURACE framework where financial and credit markets are included, interest rates will be incorporated and become endogenous.

The consumer sets his consumption according to the following consump-

⁷In a more elaborate version savings will also be made dependent on the uncertainty over income.

tion rule

$$B_{k,t}^{cons} = \begin{cases} Liq_{k,t}^{Avail} - \kappa(Liq_{k,t}^{Avail} - \Phi \cdot Inc_{k,t}^{Mean}) & \text{for } Liq_{k,t}^{Avail} > \Phi \cdot Inc_{k,t}^{Mean} \\ Liq_{k,t}^{Avail} & \text{else,} \end{cases}$$

where $\Phi \leq 1$ is a parameter, and $Inc_{k,t}^{Mean}$ is the mean individual (labor) income of an agent over the last T periods. By definition the saving propensity fulfills $0 < \kappa < 1$.

The implications of this consumption rule are as follows: if an agent has a current cash on hand that is below the fraction Φ of mean income, he spends all available liquidity and nothing is saved. If cash on hand exceeds $\Phi \cdot Inc_{k,t}^{Mean}$, the agent saves a fixed fraction in order to build up a buffer stock for bad times.

The part of cash at hand that is not saved is used as the consumption budget for that month. Each consumer goes shopping once every week, so the monthly budget is equally split over the four weeks. Parts of the weekly budget that are not spent in a given week are rolled over to the consumption budget of the following week. This yields a consumption budget $B_{k,week_t}^{cons}$ for each week in period t .

2.4.2 Selection of consumption goods

The consumer collects information about the range of goods provided. He receives information about prices and inventories. In the Marketing literature it is standard to describe individual consumption decisions using logit models. These models represent the stochastic influence of factors not explicitly modelled on consumption decisions and the power of these models to explain real market data has been well documented (see e.g. Guadagni and Little (1983)). Therefore, we rely on a model of that kind here. We assume that a consumer's decision which good to buy is random, where purchasing probabilities are based on the values he attaches to the different choices he is aware of. Denote by $G_{k,week_t}$ the set of producers whose goods consumer k has sampled in week $week_t$ of period t and where a positive stock is available at the attended mall. Since in our setup there are no quality differences between consumer goods and we also do not explicitly take account of horizontal product differentiation, choice probabilities depend solely on prices. The value of consumption good $i \in G_{k,week_t}$ is then simply given by

$$v_k(p_{i,t}) = -p_{i,t}.$$

The consumer also has the option to buy none of the goods in his sample and the utility value associated with that choice is

$$v_k^{none}(\bar{p}_{k,t-1}) = -\bar{p}_{k,t-1},$$

where $\bar{p}_{k,t-1}$ is the average price of the goods consumer k has consumed in $t - 1$. The consumer selects one good $i \in G_{k,week_t}$, where the selection probability for i reads

$$Prob_{k,i,t} = \frac{\text{Exp}[\lambda_k^{cons} v_k(p_{i,t})]}{\zeta_k^{none} \text{Exp}[\lambda_k^{cons} v_k^{none}(\bar{p}_{k,t-1})] + \sum_{i' \in G_{k,week_t}} \text{Exp}[\lambda_k^{cons} v_k(p_{i',t})]}.$$

Thus, consumers prefer cheaper products and the intensity of competition in the market is parameterized by λ_k^{cons} . Once the consumer has selected a good he spends his entire budget $B_{k,week_t}^{cons}$ for that good if the stock at the mall is sufficiently large. In case the consumer cannot spend all his budget on the product selected first, he spends as much as possible, removes that product from the list $G_{k,week_t}$, updates the logit values and selects another product to spend the remaining consumption budget there. If he is rationed again, he spends as much as possible on the second selected product, rolls over the remaining budget to the following week and finishes the visit to the mall.

2.5 Labor market

2.5.1 Labor demand

Labor demand is determined in the consumption goods market. If the firms plan to extend the production they post vacancies and corresponding wage offers. The wage offer $w_{i,t}^O$ keeps unchanged as long as the firm can fill its vacancies, otherwise the firm updates the wage offer by a parameterized fraction. In case of downsizing the incumbent workforce, the firm dismisses workers with lowest general skill levels first.

2.5.2 Labor supply

Job seekers consist of a randomly determined fraction ϕ of employed workers who search on-the-job and the unemployed. A worker k only takes the posted wage offer into consideration and compares it with his reservation wage $w_{k,t}^R$. A worker will not apply at a firm that makes a wage offer which is lower than his reservation wage. The level of the reservation wage is determined by the current wage if the worker is employed, and in case of an unemployed by his adjusted past wage. That is an unemployed worker will reduce his reservation wage with the duration of unemployment. When a worker applies he sends information about his general as well as his specific skill level to the firm.

2.5.3 Matching algorithm

According to the procedures described in the previous sections consumption goods producers review once a month whether to post vacancies for production workers. Job seekers check for vacancies. The matching between vacancies and job seekers works in the following way:

- Step 1: The firms post vacancies including wage offers.
- Step 2: Every job seeker extracts from the list of vacancies those postings to which he fits in terms of his reservation wage. Job seekers rank the suitable vacancies. The vacancy which offers the highest wage is ranked on position one and so on. If the wage offers that come with the posting are equal, vacancies are ranked by chance.
- Step 3: Every firm ranks the applicants. Applicants with higher general skill b^{gen} levels are ranked higher. If there are two or more applicants with equal general skill levels, but different specific skill levels, the applicant with the higher specific skill level is ranked higher. Based on their ranking firms send job offers to as many applicants as they have vacancies to fill.
- Step 4: Each worker ranks the incoming job offers according to the wages net of commuting costs ($comm > 0$) that may arise if he was to accept a job in the region where he does not live. Each worker accepts the highest ranked job offer at the advertised wage rate. After acceptance a worker refuses all other job offers and outstanding applications.
- Step 5: Vacancies' lists and applications' lists are adjusted for filled jobs. If a firm received refusals, these applicants are dropped from the list of applicants. If all vacancies of a firm have been filled the firm refuses the other applicants and the algorithm for this firm ends.
- Step 6: If the number of vacancies not filled exceeds some threshold $\bar{v} > 0$ the firm raises the wage offer by a fraction φ_i such that $w_{i,t+1}^O = (1 + \varphi_i)w_{i,t}^O$. If an unemployed job seeker did not find a job he reduces his reservation wage by a fraction ψ_k , that is ($w_{k,t+1}^R = (1 - \psi_k)w_{k,t}^R$). There exists a lower bound to the reservation wage w_{min}^R which may be a function of unemployment benefits, opportunities for black market activity or the value of leisure. If a worker finds a job then his new reservation wage is the actual wage, i.e. $w_{k,t}^R = w_{i,t}$. Go to step 1.

This cycle is aborted after two iterations even if not all firms may have satisfied their demand for labor. As indicated above this might lead to rationing

of firms on the labor market and therefore to deviations of actual output quantities from the planned quantities. In such a case the quantities delivered by the consumption good producer to the malls it serves is reduced proportionally. This results in lower stock levels and therefore increases the expected planned production quantities in the following period.

3 Simulation results and policy experiments

3.1 The base case

Before we illustrate the potential of our model for carrying out policy experiments with respect to the spatial distribution of policy measures we show that it generates time series of key economic variables with very plausible features. To that end we consider a base scenario which we will refer to as the *uniform low skill scenario*. Throughout the paper we assume that there are $b_{max}^{gen} = 5$ levels of general skills. The function $\chi(b_w^{gen})$, which governs the speed of specific skill improvement, is chosen such that the time workers with general skill 3 need to cut the gap between their specific skill and the firm's technology level in half is the mean of the corresponding time needed by a skill level 1 and a skill level 5 worker. An analogous linear relationship also determines the adjustment speed of workers with general skill levels 2 and 4. In a *low skill* region the skill distribution is such that 80% of workers have the lowest general skill level, whereas the remaining workers are equally distributed across the other four levels of general skills. Analogously, a region is a *medium skill* or *high skill* regions if 80% of workers have general skill level 3 respectively 5. In the uniform low skill scenario both regions are low skill regions. In addition we assume that there is a 10% probability of a quality improving innovation in the investment goods sector per month and each innovation on average increases the quality of the investment good by 5%. This corresponds to an average productivity growth rate of 6% if specific skills were sufficiently large to fully exploit all new technologies. Simulations are run for 4000 days which corresponds to about 17 years. The full set of parameters employed in this simulation is given in the Appendix. As discussed above, the main purpose of this exercise is to demonstrate the potential of our approach for carrying out spatial policy experiments and at this point no serious calibration of parameters using empirical data has been carried out. In figure 1 we show the time series for a single run of output, unemployment, (skill-dependent) wages and specific skills along the technology frontier in a typical run in the uniform low-skill scenario.

Output is increasing over time with some fluctuations. Unemployment

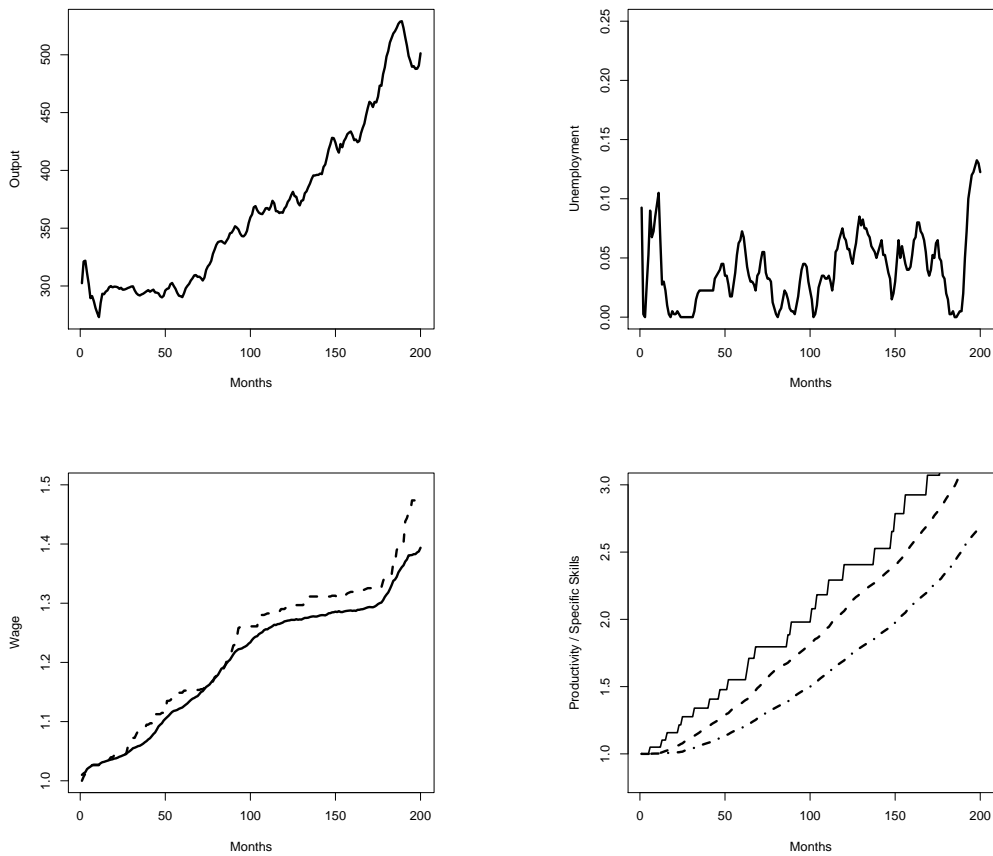


Figure 1: Single runs for the uniform low skill scenario; panels in clockwise order from upper left panel: output; unemployment rate; technology frontier (solid line), average quality of capital (dashed line) and average specific skills (dash-dotted line); average wages of workers with lowest (solid line) and highest (dashed line) general skill level;

exhibits fluctuations as well which seem to be counter-cyclical. Wages and the rate of unemployment differ between the different skill groups, where the dominant group of low-skill worker faces a higher rate of unemployment (not shown in panel). Wages of the workers with the highest skills are higher than the wages of workers with the lowest skills. Productivity improving innovations shift the technological frontier. Average quality of the capital stock also rises but is by construction below the technological frontier. Average specific skills increase also over time but constitute the limiting factor for exploiting the technological possibilities of the capital employed in the production process. This brief discussion illustrates that the model exhibits qualitative effects that are very plausible within the framework considered in our setup. Skill level differences have an impact on the individual level with respect to wages and unemployment that are well in accordance with empirical observations. Furthermore, it seems that in principle technological change that improves investment good productivity might have positive or negative effects on aggregate employment depending on the short-term rate of technological change.

3.2 Policy experiments

The framework described here allows for a number of policy experiments that seem to be of high relevance for policy makers concerned with strengthening economic growth and employment in the considered regions. As discussed in the introduction, generally speaking the model allows to evaluate policies influencing skill distributions among workers, policies influencing the speed at which the technological frontier develops and, what might be most interesting and innovative, also the interplay of policies with these two objectives.

To be more concrete, we can address questions concerning the vivid policy debate whether strengthening general or specific skills is more likely to enhance growth and employment. For example in Germany the dual-apprenticeship system is notoriously questioned by firms, unions and policy-makers with regard to its provision of general skills. A common complaint concerning university education in Germany is the high level of the abstraction of the curriculum which provides only limited specific skills. Currently there are no theoretical models that allow to analyze these issues based on thorough macroeconomic analysis. In particular standard analyses conducting cost/benefit analysis of dual apprenticeship systems are based on partial static analysis (Mühlemann et al. (2007)). Obviously, in a world with fast changing technological frontiers this does not fully take into account the full benefits of workers' general skills. Gaining better insights into the effects of increases in both types of skills should have impact on the balance of pub-

lic spending between primary and secondary education, tertiary education, life-long learning measures and dual apprenticeships.

An additional aspect in the policy debate about the optimal design of educational policies fostering innovation and growth is the question in how far such policies should depend on the technological distance of the firms in the economy from the technological frontier. Claims have been made that in regions far from the frontier the main focus should be on primary and secondary education improving the lower end of the skill distribution, whereas regions at the frontier profit more from higher investments in the tertiary sector (see Aghion (2007)). From a dynamic perspective this raises the questions in how far the effectiveness of different policy approaches depends on the speed at which the technological frontier is moving, which itself is influenced by measures in the area of innovation and technology policy. Such measures include among others direct funding of basic and applied research, financial incentives for R&D efforts by firms, providing infrastructure and incentives for R&D cooperation and intensive knowledge exchange between research institutions and firms.

The version of our framework presented here captures the effects of such policies in reduced form through the parameters γ^{inv} and Δq^{inv} . Policy efforts aiming at a speed-up of the movement of the technological frontier should lead to an increase in γ^{inv} , whereas attempts to foster basic research and to move from incremental to more fundamental innovations in the investment goods sector should trigger an increase in Δq^{inv} . Our framework allows to examine how such policies would influence the relative performance of different policies that influence the skill distribution. Understanding such cross-effects is essential to coordinate the different policy measures and to design a well balanced package of measures where the negative interaction terms between the different parts are avoided.

We illustrate the potential insights from such policy experiments by considering a simple example. Starting from the uniform low skill scenario we assume that a policy-maker responsible for economic development in both regions considers to launch a campaign in order to increase the general skill level of workers in the region. Such a campaign might involve improvements in the system of lower and higher education, providing incentives for firms to train workers, e-learning activities and so on. Furthermore, it is assumed that using the budget assigned to this campaign the policy-maker can either improve both regions from low-skill to medium-skill regions⁸ or, if all efforts are invested in only one region, improve one region to a high-skill region with

⁸According to our definition above in a medium-skill region 80% of workers have general skill level 3 and the remaining 20% are equally distributed among the other four skill levels.

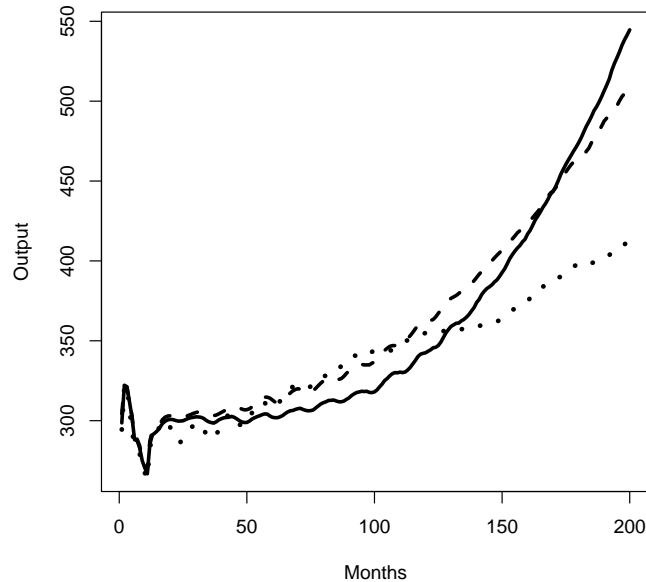


Figure 2: Batch run for outputs in uniform low scenario (dashed line), uniform medium scenario (solid line), and low/high scenario (dotted line)

the other region remaining low-skill. Since in both cases the total number of general-skill units added to the work force is identical, it is a-priori a non-trivial question whether the two policy options yield identical results and, if not, in which way the effects will differ.

In order to address this question we have run batches of 50 simulation runs for the *uniform medium* and *high-low* scenarios and compare them with each other and with the base case of uniform low-skill regions. In figure 2 we depict mean trajectories over the 50 runs in the three scenarios. As can be seen, the difference in the effect of the two policy measures is quite striking. Focussing the resources to improve the general skill level of workers in one region only (low/high scenario) yields worse results in terms of output if compared to the uniform low skill scenario. In the short run there is also a negative effect of the policy that spreads resources equally across the two regions. However, in the longer run raising the general skill level of workers in both regions yields an output that is higher than in the uniform low skill case and the low/high scenario. The large impact of the spatial allocation of policy measures in this simple example highlights the strongly non-linear and path dependent nature of a micro-founded agent-based model which leads to

non-trivial relationships between policy intervention and emergent results.

A more detailed consideration of the mechanisms underlying the different effects of these policy measures shows that the interplay of wage-dynamics, wage-driven price dynamics, and barriers to skill transfer through commuting workers that arises in the high-low scenario is responsible for the larger growth of output and employment in the uniform medium scenario.

In the low/high scenario depicted in the upper left panel of figure 3 the average specific skills increase more in the region at which the policy measure is targeted. Obviously, workers learn the specific skills more quickly as their general skills improved while no such process arises in the region without improvements in the general skills of the workers. Allocating resources to improve general skills equally across regions yields the expected results that the improvement of average specific skills is equal in both regions (upper right panel). The lower two panels give insight into the workings of the model by showing the diverging patterns of output across the two regions comparing the two policies. In the low/high scenario output increases for the region with the higher average specific skill level. Clearly, firms in this region take advantage of the more skilled workforce which allows them to exploit the technological improvement of their capital stock to a larger degree than the firms in the other region. Here, we actually observe a decline in output. Adding up regional outputs yields an increasing total output. However, total output does not increase so strongly as in the uniform medium skill scenario depicted in the lower right panel. Here, as average specific skills in both regions have increased somehow due to the equal distribution of policy efforts, output increased also in both regions. In total this has a larger impact on output in the longer run which explains why targeting the policies to only one region turns out to be the inferior policy with respect to output gains.

Looking at prices and commuting employees in the low/high scenario corroborates the analysis of our major finding of the policy experiment. Due to the faster adaptation of specific worker skills to the improving technological frontier firms in the high-skill region after a short initial phase produce with lower unit costs compared to those in the low skill region. It should be noted that this observation holds true in spite of the fact that wages in the high skill region are higher than those in the low skill region (not shown in our figures). As can be seen in the left panel of figure 4 the cost advantage translates to a lower price of the goods offered by producers from the high-skill region and this shifts demand away from producers in the low skill region towards producers in the high skill region. However producers in the high skill regions are limited in their output expansion by the lack of additional local workers. They start hiring workers from the low skill region (see the lower solid line in the right panel of figure 4), but since this is associated

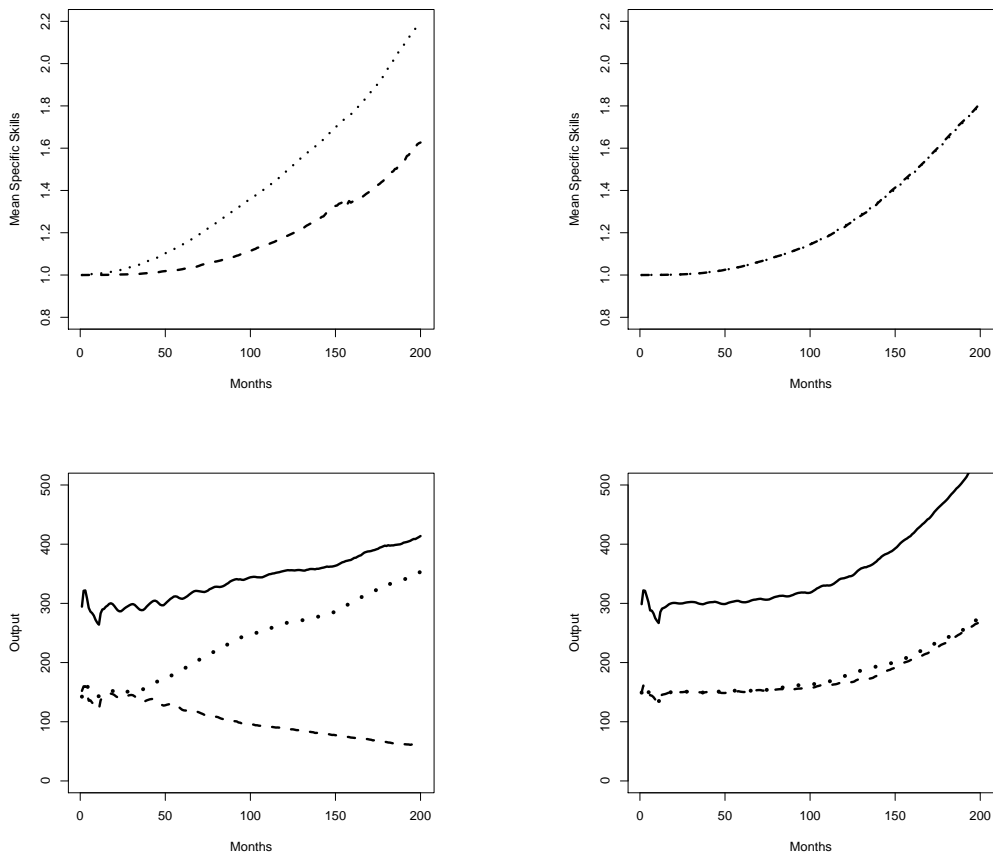


Figure 3: Batch runs for the low/high scenario (left column) and the uniform medium scenario (right column); panels in first row show specific skills in both regions, panels in second row show total output (solid line) and output in both regions;

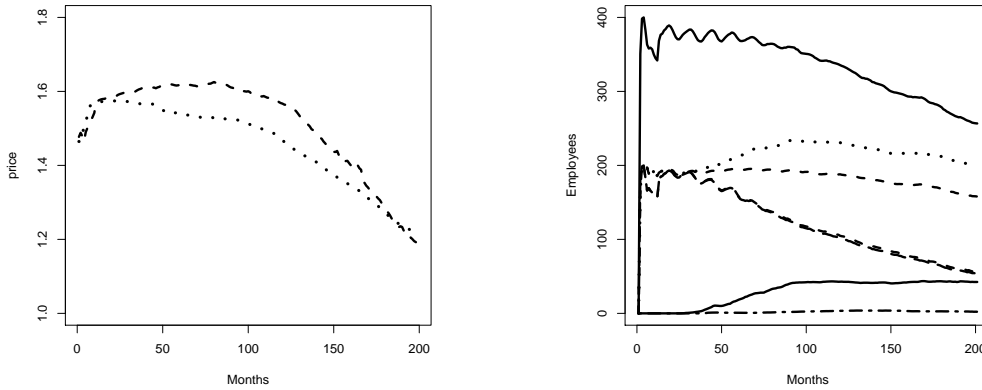


Figure 4: Batch runs for the low/high scenario; left panel shows mean prices of producers located in the high skill (dotted line) and the low skill (dashed line) region; right panel shows total employment (upper solid line), employment in the high skill region (dotted line), employment in the low skill region (middle solid line), employees in the high skill region living in that region (dashed line), commuters from the low to the high skill region (lower solid line), commuters from the high skill to the low skill region (dash-dotted line).

with labor market frictions and commuting costs for the workers, only a part of the workers dismissed by producers in the low skill region are hired in the high skill region. Therefore unemployment in the low skill region rises and total output grows at a lower rate than it would if general skill levels were uniform across regions. The right panel of figure 4 furthermore indicates that no workers from the region targeted by the policy (i.e. the high skill region) commute to the non-targeted region (dash-dotted line). To give a general economic interpretation of the observed phenomenon, we conclude that the relatively low mobility of the factor labor compared to that of consumption goods is responsible for the incomplete substitution of production in the low skill region with production in the high skill region. Furthermore, the falling demand for goods of producers in the low skill region prevents them from hiring high-skill workers from the other region and therefore no technological spillovers from the high to the low skill region emerge. Together these effects make the geographically focused policy less effective than one leading to a uniform increase of general skills in all regions.

4 Conclusions

Agent-based models are not only a useful tool to transcend borders set by standard analytical models for the study of economic systems but also open up promising avenues for economic policy design. We developed a still parsimonious micro-based macroeconomic model to study the role of innovation and skills for economic growth and employment in a regional setting. More effort has to be put into seriously calibrating our model. But still our policy experiments – which as we believe are ultimately of high relevance for policymakers concerned about the right mix of policies targeted toward improving specific or general skills, and giving firms incentives to innovate – yield very plausible insights, highlighting the role of non-trivial interaction effects in a dynamic setting which are hard to analyze in more standard static frameworks. Without stressing the results of our policy experiments too strongly there occurs to be a point in allocating resources to improve general skills equally across regions to improve output in the long run.

The next steps towards providing a software platform for policymakers that eventually will allow for ex-ante policy evaluations are to first take more serious steps towards calibrating the model. On the list of extensions to the model introducing the possibility to study product versus process innovations looms high. Finally, as pointed out earlier, this project is part of a larger endeavor. Within EURACE we aim at integrating models for the credit and financial markets build by our partners to finally arrive at a fully fledged closed macroeconomic model. Obviously, this will add many more possibilities to conduct policy analyses of the type we were trying to promote in our attempt here.

Acknowledgements

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Appendix

In table 2 the parameter setting for the simulation is summarized.

Table 2: Parameter settings

Description	Parameter	Value
Number of households:		400
Number of firms		10
Number of regions	R	2
Labor Intensity of Production	α	0.75
Labor Intensity of Production	β	0.25
Innovation probability	γ^{inv}	0.1
Depreciation rate of capital	δ	0.05
Monthly Discount factor	ρ	0.995
Production smoothing	ξ	0.5
Mark-up factor	$\frac{1}{ \epsilon_i^e -1}$	0.15
Wage update	ϕ_i	0.02
Reservation wage update	ψ_k	0.01
Minimal reservation wage	w_{min}^R	1
Marginal saving propensity	κ	0.1
Intensity of choice by consumers	λ_k^{cons}	30
Vacancy threshold	\bar{v}	2
Commuting costs	$comm$	0.2

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